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Information revelation and efficiency in auctions

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Abstract

We study the impact of information revelation on efficiency in auctions. In a constrained-efficient mechanism, i.e., a mechanism that is efficient subject to the incentive compatibility constraint, any additional information available to bidders increases the expected efficiency of the mechanism. This result cannot be extended to a more general one; a simple example shows that in a second-price sealed bid auction, revelation of information might lead to efficiency losses.

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1. Introduction

Optimal auctions are those that raise maximum revenue. Efficient auctions deliver the object to the bidder that values it the most. In a seminal paper, [Milgrom and Weber \(1982\)](#) showed that the best policy for the auctioneer is to fully reveal any relevant information about the good if the goal is to increase revenues. A natural question seems to be whether revelation of information is a good policy if the goal is to increase efficiency.¹

The answer to this question might have profound policy implications. Suppose the government plans two sales, one on the East Coast and one on the West Coast, and suppose the sets of bidders are completely different. Still, it might well be that results (including the bidding history) of the auction on one coast bear information about the object being sold on the other. Now, if the government runs the auctions

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¹ Achieving higher efficiency rather than maximizing revenues was a stated goal in many recent auctions, such as the sale of telecommunication spectrum in the United States and Britain.

sequentially, the bidders in the second one would have more information than if the auctions are simultaneous.

So, does more information lead to increased efficiency? A natural answer is probably ‘yes’. The general logic might be as follows. The less uncertainty about the object bidders face, the less is the probability that the object goes to the wrong bidder. Auctions in environments with multidimensional signals are often inefficient because of the impossibility of efficient aggregation of multidimensional information in a one-dimensional bid (Dasgupta and Maskin, 2000; Jehiel and Moldovanu, 2000).²

There are two major obstacles to obtaining a general result. The first is the absence of a focal equilibrium in a general setting. This does not allow one to trace changes in efficiency due to additional information.³ The second difficulty is the absence of a symmetric equilibrium in many natural settings with multidimensional signals (Jackson, 1999; Pesendorfer and Swinkels, 1999). We consider constrained-efficient mechanisms, i.e., mechanisms that achieve the highest efficiency subject to the constraints of incentive compatibility. We prove that disclosure of any additional information in a constrained-efficient mechanism leads to an increase in expected efficiency. However, this result cannot be extended to a general result that revealing information always leads to increasing social welfare for all types of auctions. We provide examples of situations, where revealing additional information worsens the equilibrium outcome, i.e., leads to efficiency losses or even to disappearance of a focal equilibrium. A possible explanation might be as follows. Whereas the inefficiency caused by multidimensionality reduces with disclosure of information, the inefficiency caused by interdependence between signals agents possess can increase.

This rest of the paper is organized as follows. In Section 2, it is proved that in a constrained-efficient mechanism, revelation of information does increase efficiency. Section 3 contains some examples that demonstrate that this result cannot be extended to cover second-price sealed bid auctions. Section 4 concludes.

2. The theory

To study effects of information disclosure on allocative efficiency, we start with a general model, define a constrained-efficient mechanism (Holmstrom and Myerson, 1983; Dasgupta and Maskin, 2000), and prove a general theorem for constrained-efficient mechanisms. Then, to show that the general result cannot be extended to standard auctions, we use a simple particular case, where each of two bidders receive one common and one private signal.

There are N risk neutral agents and one object for sale. Each agent receives a private multidimensional signal $s_i \in S_i \subset R^m$, and all signals are independent. The value of the object for agent i is $v_i = v_i(s_1, \dots, s_N)$. We assume that buyer i 's signal is separable between his own signal and the signals of others; that is,

² For example, suppose that both private and common components matter in bidders' valuations, and bidders know for sure their private components and observe privately some noisy signals concerning the common component. Then it is impossible to infer from a high bid whether the bidder has a high private component or is very optimistic about the common one. If only the private component matters for efficiency, then it is not always efficient to award the object to the bidder with the highest bid.

³ Goeree and Offerman (1999) argue that disclosure of some additional information leads to an increase in efficiency, interpreting additional information as an independent random summand in a common value.

there exist functions $\tau:R^m \rightarrow R$ and $\psi:R^{m(N-1)+1} \rightarrow R$ such that $v_i(s_i, s_{-i}) = \psi_i[\tau_i(s_i), s_{-i}]$ holds for all (s_i, s_{-i}) . Let Ω denote other information available to all bidders. For each vector $(t_1, \dots, t_N) \in R^m$, define

$$w_i(t_1, \dots, t_N) = E_{s_{-i}}[\psi_i(t_i, s_{-i}) \mid \tau_{-i}(s_{-i}) = t_{-i}, \Omega].$$

A constrained-efficient mechanism delivers the object to the agent with the highest $w_i(t_1, \dots, t_N)$ (Dasgupta and Maskin, 2000). We measure efficiency of a mechanism as the expected value of the object to the winner. For a constrained-efficient mechanism, this definition gives

$$W(\Omega) = \sum_{i=1}^N E v_i(s) I \left\{ w_i(\tau_i(s_i), \tau_{-i}(s_{-i})) = \max_j w_j(\tau_j(s_j), \tau_{-j}(s_{-j})) \right\},$$

where $I\{\cdot\}$ is an indicator function.

Theorem 1. *In a constrained-efficient mechanism, revealing publicly any additional information (weakly) increases efficiency.*

Proof. We have

$$\begin{aligned} W(\Omega) &= E \sum_i E_{s_{-i}} \left[v_i(s) I \left\{ w_i(\tau_i(s_i), \tau_{-i}(s_{-i})) = \max_j w_j(\tau_j(s_j), \tau_{-j}(s_{-j})) \right\} \mid \tau_{-j}(s_{-j}) = \tau_{-j}, \Omega \right] \\ &= E \sum_i E_{t_{-i}} w_i(t_i, t_{-i}) I \left\{ w_i(t_i, t_{-i}) = \max_j w_j(t_j, t_{-j}) \right\} \\ &= E \max_j w_j(t_j, t_{-j}) = E \max_j E_{s_{-j}} [v_j(t_j, s_{-j}) \mid \tau_{-j}(s_{-j}) = t_{-j}, \Omega]. \end{aligned}$$

Now suppose that $\Omega' \subset \Omega$, i.e., Ω provides more information about the object than Ω' . Then

$$\begin{aligned} W(\Omega') &= E \max_j E_{s_{-j}} [v_j(t_j, s_{-j}) \mid \tau_{-j}(s_{-j}) = t_{-j}, \Omega'] \\ &= E \max_j E [E_{s_{-j}} [v_j(t_j, s_{-j}) \mid \tau_{-j}(s_{-j}) = t_{-j}, \Omega] \mid \tau_{-j}(s_{-j}) = t_{-j}, \Omega'] \\ &\leq E E \left[\max_j E_{s_{-j}} [v_j(t_j, s_{-j}) \mid \tau_{-j}(s_{-j}) = t_{-j}, \Omega] \mid \tau_{-j}(s_{-j}) = t_{-j}, \Omega' \right] \\ &= E \max_j E_{s_{-j}} [v_j(t_j, s_{-j}) \mid \tau_{-j}(s_{-j}) = t_{-j}, \Omega] = W(\Omega), \end{aligned}$$

where the inequality follows from the fact that the expectation of the maximum of random variables is at least as large as the maximum of their expectations. □

Dasgupta and Maskin (2000) formulate sufficient conditions for the existence of a constrained-efficient mechanism. Example 1, based on their Example 5, demonstrates how such a mechanism works in the simplest possible case, and shows that revelation of information strictly increases efficiency. In this example, each of two bidders privately receives a one-dimensional signal about the common component and a one-dimensional signal about the private component of the value. Such a situation might occur, e.g., in auctioning off an oil field, where the common component is the amount of oil reserves, and private components are extraction costs.

Example 1. Each of two agents privately receives a two-dimensional signal (q_i, c_i) (all signals are independent). The values of the object to the agents are

$$v_1(q, c) = q_1 + q_2 - c_1, \quad v_2(q, c) = q_1 + q_2 - c_2.$$

There exists no efficient mechanism in this example. However, there exists a constrained-efficient mechanism, which works as follows. For expositional purposes only, assume that all signals are distributed normally with the mean 0 and standard deviation equal to 1.⁴ Denote $t_i = q_i - c_i$. Then

$$w_1(t_1, t_2) = t_1 + \frac{1}{2}t_2, \quad w_2(t_1, t_2) = t_2 + \frac{1}{2}t_1,$$

and sufficient conditions for the existence of a constrained-efficient mechanism are satisfied.

Now suppose the auctioneer releases a noisy signal about the common value,

$$x = q_1 + q_2 + \varepsilon,$$

where ε is distributed normally with mean 0 and variance σ^2 . Equivalently, agent i receives a noisy signal $x_i = q_{-i} + \varepsilon$ about his opponent's valuation. The constrained-efficient mechanism places the object in the hands of the agent with the highest $\tilde{w}_i(t_1, t_2, x)$, where

$$\tilde{w}_i(t_i, t_2, x) = t_i + E(q_{-i} | q_{-i} - c_{-i} = t_{-i}, q_{-i} + \varepsilon = x_i) = t_i + \frac{\sigma^2}{1 + 2\sigma^2}t_{-i} + \frac{\sigma^2}{1 + 2\sigma^2}x_i.$$

The decision rule inequality $\tilde{w}_1(t_1, t_2, x) \geq \tilde{w}_2(t_1, t_2, x)$ is equivalent to

$$q_1 - \frac{1 + \sigma^2}{\sigma^2}c_1 \geq q_2 - \frac{1 + \sigma^2}{\sigma^2}c_2.$$

When the variance σ^2 is finite, this decision rule is more efficient than the one that awards the object to the agent with the highest $q_i - c_i$. Moreover, the lower is the variance (the higher is the precision of the signal), the higher is the efficiency. The reason is that the higher is the weight the decision rule puts to

⁴ Dasgupta and Maskin's (2000) illustration assumes asymmetric uniform distributions.

the private signals, c_i , the more efficient is the allocation. (The first best efficiency could have been achieved if the decision rule takes only private costs into account).

Constrained-efficient and similar mechanisms are too complicated to be actively used in practice, so it is important to know how does information revelation affect efficiency in more convenient types of auctions.

Example 2. In this example, the environment is the same as described in Example 1. We consider a second-price sealed bid auction, and assume that the private fixed costs have standard normal distribution, and q_1, q_2 are normally distributed with 0 mean and variance δ^2 . Let the auctioneer announce publicly the variable q_1 . Now, the second bidder knows for sure how she values the object, whereas the first receives no additional information. It can be easily seen that a focal point consists of the following two strategies, with the strategy of the second player being weakly dominant and truthful:

$$b_1 = q_1 - (1 + \delta^2)c_1, \quad b_2 = q_1 + q_2 - c_2.$$

Here, more uncertainty (a larger δ^2) leads to greater inefficiency, while revealing information about the common component reduces inefficiency.

3. Limits to a general result

Theorem 1 supports general intuition that increasing information allows bidders' strategies to reflect the true values more closely, and thus lead to increased efficiency. However, a more general result of this kind that would cover standard auction format is impossible. Indeed, second-price sealed bid auctions are not necessarily constrained-efficient. Example 3 shows that Theorem 1 cannot be extended to cover the case of all second-price sealed bid auctions. Specifically, it demonstrates how additional information might make an equilibrium in a second-price auction less efficient.

Example 3. There are two agents and one object for sale. Agent i 's valuation of the object is $v_i = q - c_i$, where c_i is a private signal observed by i (these signals are distributed independently and normally with mean 0 and variance 1), and q is an unknown common component. Assume that private signals c_i are distributed normally with mean 0 and variance 1, and q is distributed normally with mean μ and variance δ^2 , and that all the signals are independent. Furthermore, we assume that the auctioneer knows private signals of the agents.

Proposition 1. *In Example 3, in the absence of additional information, the equilibrium in undominated strategies is efficient. Revelation of information might lead to inefficiency in an equilibrium in undominated strategies.*

Proof. If no prior information about q is available (the agents know the distribution of q only), then the following strategies constitute a symmetric equilibrium in undominated strategies: $b_i = \mu - c_i$, which is

efficient. Suppose that the auctioneer announces the signal $x=q-c_1$. Now there is the following equilibrium in undominated strategies:

$$b_1 = x,$$

$$b_2 = E(q | q - c_1 = x) - c_2 = \frac{\delta^2}{1 + \delta^2}(x - \mu) + \mu - c_2.$$

In the equilibrium, the first agent wins as long as

$$q - c_1 > \mu - (1 + \delta^2)c_2,$$

which might easily be inefficient. (Efficiency requires that the first agent wins when $c_1 < c_2$). \square

In Example 3, agents are asymmetric. That is, the auctioneer's information makes the first agent's private signal public, while bearing no information about the second agent's private signal.⁵ The example might be modified to make agents ex ante symmetric. That is, the auctioneer might announce either $q-c_1$, or $q-c_2$ with equal probabilities.⁶ Then in both post-announcement subgames, equilibria are inefficient. So, it is not the ex ante asymmetry of agents that drives the result in Example 3.

Inefficiency of an auction caused by additional information is not the only problem. Our next example, based on an example from Jackson (1999) shows that it might be that new information might lead to disappearance of a symmetric equilibria at all.

Example 4. There are two bidders in a second-price sealed bid auction. The agent i values the object at $v_i=(1/2)t_i+(1/2)q$, where t_i is a private component, which might be either 0 or 1 with equal probability, and q is a common component, which might be either 0 or w with equal probability. The value of w is unknown to the bidders and might be either $(3/16)$ with probability $(8/9)$, or 3 with probability $(1/9)$.

The agent i learns private signals t_i and s_i , where

$$P(s_i = 0 | q = 0) = \frac{3}{4}, \quad P\left(s_i = \frac{1}{2} \middle| q = 0\right) = \frac{1}{4}, \quad P(s_i = 1 | q = 0) = 0,$$

$$P(s_i = 0 | q = w) = 0, \quad P\left(s_i = \frac{1}{2} \middle| q = w\right) = \frac{1}{4}, \quad P(s_i = 1 | q = w) = \frac{3}{4}.$$

Assume that t_1, t_2, q are independent, and s_1, s_2 are independent conditional on q .

⁵ Asymmetrically informed bidders were studied in revenue maximization context in Engelbrecht-Wiggans et al. (1983), see also Krishna (2002, chapter 8).

⁶ It is essential that the bidders know whose valuation is announced.

Proposition 2. *In Example 4, in the absence of additional information, there exists an efficient symmetric equilibrium. If the auctioneer announces the value of w prior to the auction, no symmetric equilibrium exists.*

Proof. If no additional information is available, the following strategies constitute a symmetric equilibrium:

$$b_i(t_i, s_i) = \frac{1}{2}t_i + \frac{1}{2}s_i Ew = \frac{1}{2}t_i + \frac{1}{4}s_i.$$

The proof of nonexistence follows the proof of Proposition 1 in Jackson (1999), and is relegated to the Appendix A. \square

4. Conclusion

In this paper, we study the impact of information revelation on efficiency in auctions. If there exists a constrained-efficient mechanism, than any additional information revealed by the auctioneer increases expected efficiency, as measured by the expected value of the object to the winner. We show that this result could not be extended to second-price sealed bid auctions; additional information revealed by the auctioneer might reduce expected equilibrium efficiency, and even lead to nonexistence of a symmetric equilibrium. In sum, whereas the inefficiency caused by multidimensionality reduces with revelation of information, inefficiency caused by interdependence between signals agents possess, might increase.

Appendix A

Proof of Proposition 2. To complete the proof of Proposition 2, assume that when bidders know w , a symmetric equilibrium does exist. For $s_i = 0$ or $s_i = 1$, a (weakly) dominant strategy is to bid the expected value as the agent knows whether q equals to 0 or not. That is,

$$b(t = 0, s = 0) = 0, \quad b(t = 1, s = 0) = \frac{1}{2},$$

$$b(t = 0, s = 1) = \frac{3}{2}, \quad b(t = 1, s = 1) = 2.$$

Let $t = 0, s = 1/2$. Assume that with non-zero probability, the bid takes value in interval $[0, 1/2)$. Then the bidder wins, the loser either has $t = 0$ and $s = 0$ or $t = 0$ and $s = 1/2$. In the first case the expected profit of the winner is 0, but in the second case it is strictly positive, because

$$E\left(v \mid t = 0, s = \frac{1}{2}\right) = \frac{3}{4} > \frac{1}{2}.$$

So, the agents with $t=0$ and $s=1/2$ have incentives to raise the bid higher than $1/2$. However, if the bidder with $t=0$ and $s=1/2$ submits a bid higher or equal than $1/2$, then the fact that he wins is bad news, because

$$E\left(v \mid t=0, s=1/2, \text{ own bid} \geq \frac{1}{2}\right) = \frac{3}{8} < \frac{1}{2}.$$

Therefore, there is no symmetric equilibrium. □

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